UNIT 4 MATRICES

# 4.1 Matrices

## MATRIX

A matrix is a rectangular array of objects, often, numbers.

The rectangular array of numbers is a matrix having 3 rows and 2 columns.

Example (1)

## DIMENSION OF A MATRIX

Matrices having number of rows and number of columns has dimension (size) (pronounced as "m by n") and is called an matrix.

The matrix in Example 1 is a matrix since it is composed of 3 rows and 2 columns. When specifying the dimension of a matrix, the number of rows is stated first and the number of columns second.

## ELEMENTS OF A MATRIX

It is common to use an uppercase letter of the alphabet to name a matrix and the corresponding lowercase letter to name an element (entry or member) of the matrix. Subscripts are attached to the lowercase letter to specify its position in the matrix.

The first number in subscript indicates the row in which the element resides  
and the second number the column.

The subscript numbers appear adjacent to each other and typically without a comma separating them.

We could name the matrix of Example 1 with the uppercase letter and write .  
  
We specify the element in row 1, column 2, with the notation . The lowercase is used to indicate that the element is from matrix and the subscripts to indicate we are observing the entry in row 1, column 2. The subscript is not the number 12, but rather the two individual numbers, 1 and 2.

Some other elements of are

In general, the notation denotes the entry in row and column

the number in row 1, column 1

the number in row 3, column 1

the number in row 2, column 2

In general, an matrix has the form . For some number , the element is the number in row , column 2.

### TRY THESE

In the matrix

1. Specify the size of .
2. Find the value of
3. Find the value of
4. Find the value of

ANS: (a) , (b) 0, (c) 2, (d) 3

## EQUAL MATRICES

Two matrices and are said to be equal, written as , if they are the same size and all the corresponding entries are equal.

In matrix notation, for all and , if The notation names the element in row and column of matrix . Similarly, the notation names the element in row and column of matrix . The notation indicates that the element in row and column of matrix is the same as the element in row and column of matrix

## SQUARE MATRICES

A matrix is called square if it has the same number of columns as rows.

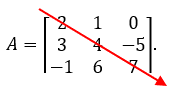
The matrices and are both equal and square.

Example (2)

and

## MAIN DIAGONAL OF A SQUARE MATRIX

Consider a square matrix, say Imagine a line passing from the top left element to the bottom right element as in the picture.



This diagonal set of elements from the top left element to the bottom right is called the main diagonal of the matrix.

### DIAGONAL AND NON-DIAGONAL ELEMENTS OF A MATRIX

The elements lying on the main diagonal of matrix are called the diagonal elements of matrix . The elements 2, 4, and 7 the diagonal elements of matrix . The elements lying off the main diagonal of matrix called the non-diagonal or off-diagonal elements of matrix . The elements and are the non-diagonal elements of matrix .

## THE IDENTITY MATRIX

An Identity matrix is a square matrix that has only 1’s on its main diagonal and 0’s everywhere else.

That is, a matrix in which every diagonal element is 1 and every non-diagonal element is 0 is an identity matrix. Identity matrices are typically named with the uppercase letter It is not uncommon to write the size of the matrix as a subscript on the

The square matrix is the . We could write to indicate the identity matrix.

Example (3)

## THE ZERO MATRIX

The zero matrix is a matrix, in which every element is 0.

Zero matrices are commonly named with a 0.

The matrix is a zero matrix.

Example (4)

## THE TRANSPOSE OF A MATRIX

Consider some matrix For example, suppose is the matrix .  
Form a new matrix, call it -transpose and denote it by , by making

* The first row of the first column of ,
* The second row of the second column of .

Then is the transpose of .

The rows of a matrix are the columns of its transpose. If the matrix is size ,  
then dimension of is .

## ROW MATRICES AND COLUMN MATRICES

A row matrix is a matrix with only one row and any number of columns.

The matrix is a row matrix with 3 columns. It is a matrix.

A column matrix is a matrix with only one column and any number of rows.

The matrix is a column matrix with 2 rows. It is a matrix.

## VECTORS AS MATRICES

When we first described vectors, we expressed them using the bracket notation. For example, we could write a vector as . We can just as easily describe this vector using a row matrix or column matrix

## EXAMPLES

1. Specify the dimension of each matrix.
   1. ANS:
   2. ANS:
   3. ANS:
2. True or False: The transpose of a square matrix is also a square matrix.

ANS: True

1. In the matrix specify
   1. Find the value of
   2. Find the value of
   3. Find the value of
   4. Find the value of

ANS: (a) 5, (b) 2, (c) 1, (d) 4

1. Construct and name the transpose of .

ANS: .

1. Construct

ANS: .

1. Construct the transpose of

ANS:

1. Write the column matrix using vector bracket notation, < >.

ANS: <4,3,2>

1. Construct a matrix in which the diagonal elements are 5 and 6 and the non-diagonal elements are 0 and 2.

ANS: or

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